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*Conjugacy separability of generalized free products of certain conjugacy separable groups.* (English)

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A group  $G$  is said to have unique root property for elements of infinite order if  $x^n = y^n$  implies  $x = y$  for all  $x, y \in G$  of infinite order ( $n \in \mathbf{N}$ ); a subgroup  $H$  of  $G$  is said to be isolated if  $x^n \in H$  implies  $x \in H$  for all  $x \in G$  ( $n \in \mathbf{N}$ ). Let  $A, B$  be finitely generated free-by-finite or nilpotent-by-finite groups. Let  $G = A *_H B$  with  $H = \langle h \rangle$  cyclic. If  $A$  and  $B$  both have the unique root property for elements of infinite order or if  $H$  is isolated in both  $A$  and  $B$  then  $G$  is conjugacy separable, that is, if  $x \not\sim y$  in  $G$  then there is a normal subgroup  $N$  in  $G$  of finite index such that  $\bar{x} \not\sim \bar{y}$  in  $\bar{G} = G/N$ . As a corollary, groups of  $F$ -type are conjugacy separable.

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